Process Simulation and Optimal Design of Membrane Separation System
for CO₂ Capture from Natural Gas

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Abstract: In order to avoid carbon dioxide (CO$_2$) built up in the atmosphere, the major source of global warming, CO$_2$ capture must be applied to large point sources including natural gas processing. Membrane process, a relatively new technology among other available techniques, can be used for the purpose of CO$_2$ capture from natural gas. Over the decades, the membrane performance has been described by different mathematical models, but there is limited work done in the field of process simulation where membrane models can be incorporated with other unit operations using a commercially available simulator. In this paper, mathematical model for cross flow membrane separation has been proposed to be incorporated with ASPEN HYSYS as a user defined unit operation in order to design and optimize the membrane system for the separation of CO$_2$ from natural gas. The proposed simulated model is validated by published experimental and simulated data. Parameter sensitivities, along with process economics, have been studied by changing the operating conditions (feed composition and pressure) and membrane selectivity for different design configurations such as single stage (with and without recycle) and multiple stages (with permeate and retentate recycle) systems. It has been observed that double stage with permeate recycle system gives the optimum design configuration due to minimum process gas cost involved with it. The ASPEN HYSYS user defined unit operation proposed in the current paper has potential to be applied for the design, optimization and scale up of complex membrane systems.

Keywords: CO$_2$ capture; Membrane Process; Membrane modeling; Process simulation
Nomenclature

$A_m$  Total membrane area ($m^2$)

BPC  Base Plant cost (USD)

CC  Installed Compressor cost (USD)

CH$_4$LS  Annual cost of methane loss in permeate (USD/year)

CMC  Annual contract and material maintenance cost (USD/year)

CRC  Annual capital related cost (USD/year)

DL  Direct labor cost (USD/year)

FC  Fixed cost (USD)

GPC  Gas processing cost (USD/MSCFD of natural gas product)

HP  Power requirement for compressors (hp)

J  Gas permeation flux through membrane (MMSCF/ft$^2$ day)

$L_f$  Feed flow rate (mol/s)

$L_r$  Retentate flow rate (mol/s)

LOC  Annual labor overhead cost (USD/year)

LTI  Annual local tax and insurance cost (USD/year)

l  Membrane thickness (mil)

MC  Total cost of membrane modules (USD)

MMBTU  $10^6$ BTU

MMSCFD  $10^6$ ft$^3$/day

MRC  Annual membrane replacement cost (USD/year)

MSCF  $10^3$ standard cubic feet (at standard temperature and pressure)

NGLS  Annual loss of natural gas (MMSCF/year)

NHV  Heating value of natural gas (1066.8 MMBTU/MMSCF)

NWP  Wellhead price of crude natural gas (USD/MMBTU)
OSF  On stream factor

P  Project contingency (USD)

P_A  Permeability of component A (mol/MPa-m^2-s)

P_B  Permeability of component B (mol/MPa-m^2-s)

p_h  Pressure on the high pressure side (bar)

p_l  Pressure on the low pressure side (bar)

SC  Start up cost (USD)

SCF  Standard cubic feet (at standard temperature and pressure)

TFI  Total facilities investment (USD)

TPI  Total plant investment (USD)

t  Membrane life (years)

UC  Annual utility cost (USD/year)

UCP  Utility cost (USD/kwh)

VOM  Annual variable operating and maintenance cost (USD/year)

V_p  Permeate flow rate (mol/s)

x_f  Feed mole fraction

x_0  Retentate mole fraction

y_p  Permeate mole fraction

Greek Symbols:

Θ  Stage cut or fraction permeated

α  Selectivity of the membrane

η_{cp}  Compressor efficiency (%)
1. INTRODUCTION

The increasing world-wide energy demand and pricing trends have directed the attention of oil and gas companies towards developing contaminated fields. On the other hand, global perceptions on climate change are exercising constant pressure on energy companies to adopt practices leading to the reduction of carbon emissions (Hart and Gnanendran, 2009). Therefore, CO₂ capture is attracting interest as an option for minimizing CO₂ emissions from the use of fossil fuels (Steeneveldt et al., 2006).

The amount of CO₂ contents in the natural gas can vary from 4% to 50% depending on the gas source. Before the transportation of natural gas, it must be pre-processed in order to meet the typical pipeline specification of 2%-5% CO₂ (Datta and Sen, 2006; Safari et al., 2009). Currently, many natural gas wells are undeveloped due to their low production rate and poor quality, i.e., the high CO₂ content, which has created the necessity to develop efficient processes for the separation of CO₂ from natural gas (Lee et al., 1995).

CO₂ can be removed by a number of processes considering the factors of; capital and operating costs, gas specifications and environmental concerns. The major processes can be grouped as follows:

- Absorption Processes (Chemical and Physical absorption)
- Adsorption Process (Solid Surface)
- Hybrid Solution (Mixed Physical and Chemical Solvent)
- Physical Separation (Membrane. Cryogenic Separation) (Maddock, 1982; Koros and Chern, 1987)

Membranes processes represent commercially proven technology for natural gas processing application. For a gas to permeate through a membrane surface, the gas must first
dissolve in the high-pressure side of the membrane, diffuse across the membrane wall, and evaporate from the low-pressure side. Gas separation therefore works on the principle that some gases are more soluble in, and pass more readily through polymeric membrane than other gases (Geankoplis, 2003; Baker, 2004; Ebenezer, 2005).

In the membrane process, feed gas is pretreated before entering the membrane system in order to ensure an efficient operation. It serves mainly to control the fouling, plasticization and condensation of hydrocarbons in the membranes (Baker and Lokhandwala, 2008; Xomeritakis et al., 2007). Moreover, the temperature control system is provided to maintain the gas at the desired operating temperature of the membrane fibres. Finally, the heated gas is entered into the membrane gas separators where it gets separated into two streams: the permeate, a low pressure CO₂ stream and the non-permeate or residue, a high pressure hydrocarbon rich stream (Ebenezer, 2005).

Although membrane separation technology has become a major industrial application only during the last few decades but the study of gas separation has a long history (Baker, 2004). Graham (1866) measured the permeation rates of all the gases known by that time through different diaphragms (Baker, 2004). Amerongen (1950), Barer (1951) and Stern (1966) played an important role in the development of solution diffusion model for the explanation of gas permeation (Baker, 2004). The first company to establish a Prism membrane was Monsanto that marketed for hydrogen separation, but the success of Monsanto encouraged other companies, like Cynaoi Separex and Grace Membrane Systems, to produce membrane plants for natural gas processing (Hennis et al., 1980; Baker, 2004).

Further research was conducted by Lee et al. (1994) who made field tests of membrane modules for the separation of carbon dioxide from low-quality natural gas. In their study they investigated the effects of the operating variables of pressure, feed flow rate, and the carbon
dioxide concentration in the feed. In addition to the analysis of the field data, computer models were applied for the separation of gases under perfect mixing and cross flow conditions. Lababidi et al. (1996) developed the mathematical model to optimize three configurations including single stage, two stages, and the continuous membrane column (CMC) whereas Qi and Hensen (1998) developed the optimal design strategy for spiral membrane networks for gas separations. Moreover, Qi and Hensen (2000) proposed mixed integer non linear programming for the membrane separation of multicomponent gas mixtures.

Wang (2004) enhanced the operational flexibility and adaptability of membrane process using an optimal method in which auto-controlling of the permeate gas flux was applied for the first time. Furthermore, Datta and Sen (2006) worked on the optimization of the gas processing cost for a membrane unit demonstrating that the optimum configuration might be unique within the certain ranges of CO$_2$ concentration and the minimum gas processing cost could only be achieved by adjusting the number of modules in each stage and the compressor power. The permeability and selectivity variations of the CO$_2$/CH$_4$ system, which included both temperature and pressure effects simultaneously, have been thoroughly studied by Safari et al. (2008). In addition, Hau et al. (2008) have investigated process design, economics, and sensitivity of the membrane stage with recycle streams.

The current paper provides analysis of different design parameters for membrane gas separation under different configurations using ASPEN HYSYS software. As membrane unit is not a pre-defined unit operation in ASPEN HYSYS, a cross flow model is proposed to predict the membrane performance in the CO$_2$ separation from natural gas. Finally, the proposed model is included in the process simulation as user defined unit operation along with other available unit operations. The main purpose is to optimize the membrane system configuration for
different feed compositions (from low CO\textsubscript{2} to high CO\textsubscript{2} contents), feed pressures (from low to very high pressure) and membrane selectivity.

2. METHODOLOGY

2.1. Transport Mechanism

The solution diffusion model is the most widely accepted transport mechanism for gas separation through polymer membranes. According to this model, permeants dissolve in the membrane material and then diffuse through the membrane with a concentration gradient. A separation is achieved as a result of difference in the amounts of material that dissolves in the membrane and the rate of material diffusion through the membrane. In a gas separation, a mixture of gases at a pressure \( p_0 \) is applied to the feed side of the membrane, while the permeate gas at is removed a lower pressure \( p_i \) from the downstream side of the membrane. (Wijmans and Baker, 1995). The governing flux equation (Eq. (i)) is given by Fick's law of diffusion where driving force is partial pressure difference over the membrane.

\[
\frac{q_{pi}}{A_m} = \frac{q_{p}y_{pi}}{A_m} = I_i = \frac{p_i}{l} (p_h x_i - p_l y_i)
\]  

(i)

Where \( J \) (m\textsuperscript{3}/m\textsuperscript{2}h) is the flux of gas component \( i \), \( q_p \) is the volume of the permeating gas (i) (m\textsuperscript{3}/h), \( P_i \) is the permeability of gas component \( i \) ((m\textsuperscript{3}/m\textsuperscript{2}h.bar), \( P_h \) and \( P_l \) are feed and permeate side pressures (bar), \( x_i \) and \( y_i \) are the fractions of component \( i \) on the feed and permeate sides and \( A_m \) (m\textsuperscript{2}) is the membrane area required for the permeation.(Hussain and Hagg, 2010). The permeability (P) can be expressed as

\[
P = D_{AB} \cdot S
\]  

(ii)
Where $D_{AB}$ (m$^2$/s) is the diffusivity and $S$ (m$^3$(STP)/m$^3$.bar) is the solubility coefficient for the gas in the membrane. The ratio of pure gas permeabilities ($P_A, P_B$) gives the separation factor or membrane selectivity, $\alpha$ (Geankoplis, 2003).

$$\alpha = \frac{P_A}{P_B}$$  \hspace{1cm} (iii)

It is important to mention here that Eq. (i) can be used to accurately and predictably rationalize the properties of gas permeation membranes (Wijmans and Baker, 1995).

### 2.2. Process Simulation Method

In this work, a cross flow isothermal model (Figure 1) has been implemented to describe the performance of a membrane module. The model is then interfaced with Process simulation programme, ASPEN HYSYS in order to calculate permeate and retentate of the system with any number of modules, allowing complex process simulations. The programme has the possibility to use ASPEN HYSYS capabilities to calculate mass and energy balances and combine in the process model. The important process parameters are flow rates, temperatures, compositions, pressure ratio (between the upstream pressure $p_h$ and downstream pressure $p_l$ over the membrane) and stage cut (ratio of permeate $V_p$ to feed flow rate $L_f$). The recovery of desired component (methane in our work) is calculated as

$$R = \frac{\Theta y_i}{x_i}$$ \hspace{1cm} (iv)

Where $\Theta$ is the stage cut and $x_i$ and $y_i$ are feed and permeate fractions of the desired component respectively.

The model assumes no mixing in the permeate side as well as on the high pressure side. Thus, the composition of permeate can be determined at any point along the membrane by the relative
permeation rates of feed component at that point. In addition, the assumptions that follow the suggested model are:

1. It holds only for the binary gas mixture.
2. The feed side pressure of each stage is equal to the pressure of the feed stream.
3. Membrane permeability is independent of the pressure and temperature.
4. The feed side pressure drop is negligible for each stage.
5. The system operates at isothermal conditions.

For a binary gas mixture, the local permeation rate at any point in the stage over a differential membrane area \(dA_m\), as shown in figure 1, is as follows

\[
ydV = \frac{P_A}{t} \left[ p_h x - p_l y \right]
\]  

\[
(1 - y)dV = \frac{P_B}{t} \left[ p_h (1 - x) - p_l (1 - y) \right]
\]  

Dividing eq (i) by eq (ii), we get

\[
\frac{y}{1-y} = \frac{\alpha [x - (p_l - p_h)y]}{(1-x) - \left(\frac{p_l}{p_h}\right)(1-y)}
\]  

(vii)

Where \(P_A\) and \(P_B\) are the permeabilities of pure gas components (CO\(_2\) and CH\(_4\) in this work), \(x\) and \(y\) are the feed and permeate composition at any point along the membrane, \(t\) is the membrane thickness and \(\alpha\) is the membrane selectivity (Geankoplis, 2003). The above set of differential equations were solved using VB code which is used as a subroutine in ASPEN HYSYS in order to calculate the purity (permeate mole fraction \(y_p\)), methane (CH\(_4\)) recovery, and membrane area \(A_m\) required for the separation. These parameters, along with compressor
power, define the gas processing cost (GPC) for the membrane system. In order to get the optimal design, it must be minimized keeping operating conditions under consideration.

2.3. **Design Configurations**

The design of a membrane separation process depends on the operating parameters of the individual permeators as well as the configuration of permeators (Qi and Hensen, 1998a). For moderate purity and recovery requirement, a single stage system, with and without recycle is appropriate (Schell and Houston, 1982). For more demanding separations, a multiple stage system is required that can further be modified by recycling permeate or retentate stream (Spillman et al., 1988; Coady and Davis, 1982).

The design of multiple stage system is very complex as it is not feasible to consider all possible configurations (Koros and Chern, 1987; Spillman, 1989; Qi and Hensen, 1998a). The conventional approach is to select a small number of design configurations and optimize the operating conditions of each configuration. The final optimum design is chosen to be the system with most favourable economics (Spillman et al., 1988; Babcock et al., 1988; Bhide and Stern, 1993; Qi and Hensen, 1998a).

The proposed design configurations include single stage (SS), single stage with permeate recycle (SSPR), double stage with permeate recycle (DDPR), double stage with retentate recycle (DDRR), triple stage with retentate recycle (TTRR) and triple stage with permeate and retentate recycle (TTPRR) as shown in Fig. 2a-2f. A compressor is needed at the start of each configuration in order to achieve the desired pressure for the parametric investigation. In addition, a smaller compressor is required to increase the pressure of permeate stream before recycling. The cooler is needed after each compression stage in order to decrease the temperature of feed stream to avoid membrane damage.
2.4. Process Conditions and Economic Parameters

The composition, flow rates, pressures and temperature of crude natural gas depend mainly on the source therefore feed conditions that are typical for medium sized natural gas treatment plant are selected. As a result, the feed flow rate of crude natural gas is maintained at 35 MMSCF (Hao et al, 2002). On the other hand, a wide range of feed pressures (10-100 bar) and membrane selectivity (5-80) has been investigated. The outlet residue CO$_2$ concentration is set to 2% while outlet permeate pressure for each stage is not greater than 4 bar (Qi and Hensen, 1998a). The thickness of membrane is considered to be 1000 Å (3.937 × 10$^{-6}$ in) (Hao et al, 2002). In addition, it is assumed that maximum outlet temperatures in the compressors is limited to 150°C giving the compression ratio of 3.5 over each compressor stage (Hussain and Hagg, 2010).

The processing cost for natural gas is often expressed as the cost per MSCF of feed but it is more reasonable to define the processing cost per MSCF of product due to presence of substantial amount of CO$_2$ in the feed. In addition, upgraded natural gas is sold on the basis of product volume rather than of feed volume (Hao et al, 2002). Therefore, processing cost per MSCF of product is used in the present study.

The procedure to calculate the gas processing cost (GPC) is given in Table 1. It includes the capital related cost (CRC), the variable operating and maintenance cost (VOM) and the cost of CH$_4$ lost in the permeate stream (CH$_4$LS) (Hao et al, 2008; Hussain and Hagg, 2010). The cost of cooling system is included in the compressor cost (CC) as it usually comes along with compressors. A payout time is considered to be 5 years in order to calculate the capital cost whereas project contingency, that covers the unpredictable elements of the project, is assumed to be 20% of the base plant cost (Hao et al, 2008).
3. RESULTS AND DISCUSSIONS

3.1. Model Validation

The suggested simulated mathematical model is validated by published experimental and simulated data for CO$_2$ removal from natural gas using membrane separation processes. The data by Pan (1986) is based on the experiments performed on sour natural gas. The feed gas used in the experiments contains 48.5% CO$_2$ that is removed in the permeate stream in order to increase the recovery of methane in the retentate stream. The temperature and pressure values of the gas are 10ºC and 35.28 bars, respectively, while the permeate pressure is 9.28 bar. The selectivity is assumed to be 25. The same process conditions are maintained for the proposed simulated model and compared with experimental data by Pan (1986). Table 2 shows that the suggested model gives good approximation to the experimental data with maximum percentage error < 7%. The small error in the comparison could be attributed to the sensitivity of membrane permeability towards high pressure, which is assumed negligible in the suggested mathematical model.

The proposed simulated model is further validated by the data from Qi and Hensen (1998a) based on the study conducted on CO$_2$ separations from natural gas using approximate algebraic permeator model. The operating conditions and requirements are maintained in such a way to match that of simulated data by Qi and Hensen (1998a). The CO$_2$ concentration in the feed gas is set to 20% while permeate pressure is not allowed to exceed than 10.5 bar in order to avoid negative pressure operation. The temperature of feed gas is 40ºC and the selectivity of membrane is considered to be 20. Furthermore, natural gas processing capacity is maintained at 19353 m$^3$/day (6.8*10$^5$ ft$^3$/day) for the simplest design configuration of single stage membrane system without any recycle stream. Table 3 shows that the simulated model
proposed in our work is in close agreement with the simulated data by Qi and Hensen with maximum percentage error < 5%.

3.2. Parametric and Economic Analysis

3.2.1. Methane Recovery:

Methane (CH₄) recovery decreases with the increase in CO₂ contents of the feed (Qi and Hensen, 1998). At the same time, CH₄ recovery can be improved by recycling the permeate stream as well as by using multiple stage configuration (Schell and Houston, 1982; Babcock et al., 1988; Spillman et al., 1988).

Fig. 3 shows the effect of feed composition on CH₄ recovery for all proposed configurations, for the stage cut of 0.5 and selectivity of 25. The permeability of CH₄ is considered as 1.4×10⁻³ mol/MPa-m²-s while the feed pressure and permeate pressure are maintained at 100 and 4 bar, respectively. It can be observed that the CH₄ recovery is reducing with the increase of CO₂ in the feed gas. The system without recycle, as expected, provides the lowest methane recovery. It can also be observed that methane recovery for single stage system with recycle is almost same as that of single stage system without recycle so it is not favourable to recycle the permeate stream in single stage system. Besides, the simulated results also show that the usage of a multiple stage systems leads to high methane recovery. In addition, it can be deduced that methane recovery can be improved by recycling permeate and retentate stream in the case of multiple stage systems.

Fig. 4 shows the effect of feed pressure on CH₄ recovery for different configurations. The stage cut and selectivity is same as in the previous case, whereas the feed gas contains 20% CO₂ and 80% CH₄. It can be observed that the increase in feed pressure improves CH₄ recovery. It is due to the fact that the increased pressure creates a greater driving force across the
membrane. As a result, a net increase in permeation through the membrane increases methane recovery.

Membrane properties have a high influence on CH$_4$ recovery, which increases with the increase in selectivity of the membrane. The reason is that increased selectivity leads to higher permeation and thus to an improved methane recovery. Fig. 5 shows the effect of membrane selectivity on the three proposed configurations. As expected, the increase in selectivity increases CH$_4$ recovery, especially for the multiple stage configurations. On the other hand, the increment in selectivity for the single stage configurations (with and without recycle) is less significant on the methane recovery, especially for higher selectivity membranes.

3.2.2. Total membrane Area

The effect of feed composition on the total membrane area required for the effective separation is studied for proposed design configurations as shown in Fig 6. It is observed that the total membrane area increases with the increase in CO$_2$ composition of the feed until it reaches its maximum point. After that, a further increase can lead to the decrease in the membrane area requirement. It is due to the characteristics of chosen selectivity of the membrane. It can also be observed that recycling the retentate stream in the multiple stage configurations can lead to large requirements of area, while in the single stage system, recycling has minimal effect.

On the other hand, an increase in feed pressure would decrease the total membrane area required for the effective separation as shown in the Fig. 7. It is obvious that high pressure leads to a high rate of permeation, due to which less membrane area is required for the separation.
Fig 8. shows the effect of membrane selectivity on the total membrane area for different design configurations. Increasing selectivity decreases the membrane area requirements, which is more pronounced in the multiple stage configurations, followed by single stage configuration with recycle and single stage configuration without recycle.

3.2.3. Gas Processing Cost:

In order to find the optimal design, gas processing cost (GPC) must be minimum subject to operating conditions, material and energy balances, and individual permeator mathematical model (Qi and Hensen, 1998a). The effect of feed composition on the GPC for the proposed design configurations is shown in Fig. 9. It can be noted that single stage systems without recycle (SS) yield a moderate GPC because the membrane area required is small and no compressors are needed. The double stage with retentate recycle (DSRR) and triple stage with permeate and retentate recycle (TSPRR) has the maximum GPC even in the presence of high methane recovery due to the high compressor power and very large membrane area required. Triple stage with retentate recycle (TSRR) yields relatively less GPC due to improved methane recovery. The minimum GPC is achieved by the double stage system with permeate recycle because of the high methane recovery and moderate power requirement for the configuration.

Moreover, it can also be observed that the increase of CO₂ contents in the feed gas leads to high GPC until a certain optimum point, depending upon the operating conditions and the membrane properties. The further increase of CO₂ contents can lead to the decrease in the GPC. It is due to the similar behaviour of total membrane area requirement with the change in CO₂ contents of the feed (discussed in section 3.2.2).

The effect of feed pressure on the GPC is shown in the Fig. 10. The increase in feed pressure improves the GPC, especially at relatively lower pressure ranges, due to the
improvement in methane recovery and less membrane area required for the separation at increased feed pressure.

The effect of selectivity on GPC is shown in Fig. 11. It can be deducted that GPC decreases significantly with the increase in selectivity of the membrane, which can be explained by the fact that membranes with high selectivity yield high methane recovery with less requirements of membrane area. These results are consistent with those obtained by Spillman et al. (1988), Babcock et al. (1988) and Qi and Hensen (1998a).

It can be observed in GPC comparison for different design configurations that the optimal design for CO₂ capture from natural gas using membrane is double stage with permeate recycle as it gives minimum GPC due to high methane recovery and less requirement of membrane area (even for feed with high contents of CO₂).

4. CONCLUSIONS

A systematic design strategy has been presented for the CO₂ capture from natural gas using a membrane process. The proposed cross flow model is included in the process simulation (Aspen HYSYS) as a user defined unit operation along with other available unit operations in order to design the membrane system configuration. The simulated model is validated with experimental data, where the simulated data exhibit good agreement with the published results. The design sensitivity has been investigated by changing the operating conditions and the membrane properties. It is observed that gas processing cost (GPC) increases with the increase in composition of CO₂ in natural gas to a certain point. After that, further increase in CO₂ contents can lead to the minimization of GPC. Moreover, it can be minimized by the increase in feed pressure or selectivity of the membrane. Different configurations including single stage (with and without recycle) and multiple stage membrane
systems (with permeate and retentate recycle) have been investigated for optimal design under the present study. The findings indicate that the GPC is minimum for double stage membrane system with permeate recycle making it the optimal design for the membrane separation system. Furthermore, the Aspen HYSYS user defined unit operation has potential to be applied for complex membrane system design and optimization study.

Acknowledgements

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LISTS OF TABLES

Table 1: Economics parameters for gas processing cost (Hao et al., 2008)
**Total Plant Investment (TPI):**

\[ TPI = TFI + SC \]

<table>
<thead>
<tr>
<th>Component</th>
<th>Formula/Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Membrane module cost (MC)</td>
<td>$ 5/ft^3</td>
</tr>
<tr>
<td>Installed compressor cost (CC)</td>
<td>$ 8650 *(HP/Ƞ_{cp})^{0.82}</td>
</tr>
<tr>
<td>Fixed cost (FC)</td>
<td>MC + CC</td>
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<tr>
<td>Base Plant Cost (BPC)</td>
<td>1.12 * FC</td>
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<tr>
<td>Project Contingency (PC)</td>
<td>0.20 * BPC</td>
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<tr>
<td>Total facilities investment (TFI)</td>
<td>BPC + PC</td>
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<tr>
<td>Start up cost (SC)</td>
<td>0.10 * VOM</td>
</tr>
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</table>

**Annual Variable Operating and Maintenance Cost (VOM):**

\[ VOM = CMC + LTI + DL + LOC + MRC + UC \]

<table>
<thead>
<tr>
<th>Component</th>
<th>Formula/Description</th>
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<tr>
<td>Contract and Material Maintenance Cost (CMC)</td>
<td>0.05 * TFI</td>
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<tr>
<td>Local Taxes and insurance (LTI)</td>
<td>0.015 * TFI</td>
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<tr>
<td>Direct Labor cost (DL)</td>
<td>$ 15/h</td>
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<tr>
<td>Labor Overhead Cost (LOC)</td>
<td>1.15 * DL</td>
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<tr>
<td>Membrane Replacement Costs (MRC)</td>
<td>$ 3/ft^2 of membrane</td>
</tr>
<tr>
<td>Utility Cost (UC)</td>
<td>$ 0.07/kwh</td>
</tr>
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</table>

**Annual Cost of CH₄ Lost in Permeate (CH₄LS):**

\[ CH₄LS = NGLS * NHV * NWP \]

<table>
<thead>
<tr>
<th>Component</th>
<th>Formula/Description</th>
</tr>
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<tbody>
<tr>
<td>Annual Natural Gas Lost (NGLS)</td>
<td>NGLS = 365 * OSF * L_f * y_p(CH₄) * x_f(CH₄)</td>
</tr>
</tbody>
</table>

**Gas Processing Cost (GPC):**

\[ GPC = (CRC + CH₄LS + VOM) / [365 * OSF * L_f * (1 - SCE) * 1000] \]

<table>
<thead>
<tr>
<th>Component</th>
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<tr>
<td>Annual Capital Related Cost (CRC)</td>
<td>0.2 * TPI</td>
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<tr>
<td>Membrane Life (t)</td>
<td>4 years</td>
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<tr>
<td>Wellhead Price of Crude Natural Gas</td>
<td>$ 2/MMBTU</td>
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<td>Heating Value Of Natural Gas</td>
<td>1066.8 MMBTU/MMSCF</td>
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<tr>
<td>On stream factor (OSF)</td>
<td>96 %</td>
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<tr>
<td>Compressor Efficiency (Ƞ_{cp})</td>
<td>0.8</td>
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Table 2: Validation of mathematical model with published experimental data by Pan (2008)
Table 3: Validation of mathematical model with simulated data by Qi and Hensen (1998a)

<table>
<thead>
<tr>
<th>Feed Pressure (bar)</th>
<th>Proposed simulated model</th>
<th>Experimental data by Pan (2008)</th>
<th>% Error</th>
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<tr>
<td>0.40</td>
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Fig. 1. Schematic diagram of cross flow membrane separation

Fig. 2a. Process flow diagram (PFD) in ASPEN HYSYS for design configuration having single stage (SS)

Fig. 2b. Process flow diagram (PFD) in ASPEN HYSYS for design configuration having single stage with permeate recycle (SSPR)
Fig. 2c. Process flow diagram (PFD) in ASPEN HYSYS for design configuration having double stage with permeate recycle (DSPR)

Fig. 2d. Process flow diagram (PFD) in ASPEN HYSYS for design configuration having double stage with retentate recycle (DSRR)

Fig. 2e. Process flow diagram (PFD) in ASPEN HYSYS for design configuration having triple stage with retentate recycle (TSRR)
Fig. 2f. Process flow diagram (PFD) in ASPEN HYSYS for design configuration having triple stage with permeate and retentate recycle (TSPRR)

Fig. 3. Effect of feed composition on methane recovery

CO₂ Contents in Feed, X_f

CH₄ Recovery, R (%)
Fig. 4. Effect of feed pressure on methane recovery

Fig. 5. Effect of membrane selectivity on methane recovery
Fig. 6. Effect of feed composition on total membrane area

Fig. 7. Effect of feed pressure on total membrane area
Fig. 8. Effect of membrane selectivity on total membrane area

Fig. 9. Effect of feed composition on gas processing cost
Fig. 10. Effect of feed pressure on gas processing cost

Fig. 11. Effect of membrane selectivity on gas processing cost